Space Chips

The picture below shows a cuboctahedron (thanks to Wikimedia foundation):



Every corner looks the same: as you go around it, you see a triangle, a square, a triangle, and a square. By counting the number of sides of each of these shapes that meet at any corner, we can call it a (3,4,3,4) polyhedron. Or we can say "The recipe for a cuboctahedron is (3,4,3,4)."

- 1. Make a model of a cuboctahedron.
- 2. How many triangles and how many squares are needed to make a cuboctahedron?
- 3. By building the shapes, fill in the chart on the next page. Warning: some of those recipes are impossible!
- 4. Which recipes are impossible? How can you tell? Is there a way to predict, just by looking at the recipe, whether it's going to work?
- 5. Think up some more recipes of your own and try them out!
- 6. Is there a way to predict how many triangles, squares, and pentagons you'll need, just by looking at the recipe and doing some calculations, without actually building the shape?

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Recipe	Triangles	Squares	Pentagons	Name
(3,4,3,4)				Cuboctahedron
(4,4,4)				
(3,3,3)				
(5,5,5)				
(3,3,3,3)				
(3,5,3,5)				
(4,5,4,5)				
(3,3,3,3,3)				
(3,4,5)				
(3,4,3,5)				
(3,3,5)				
(3,3,3,5)				

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